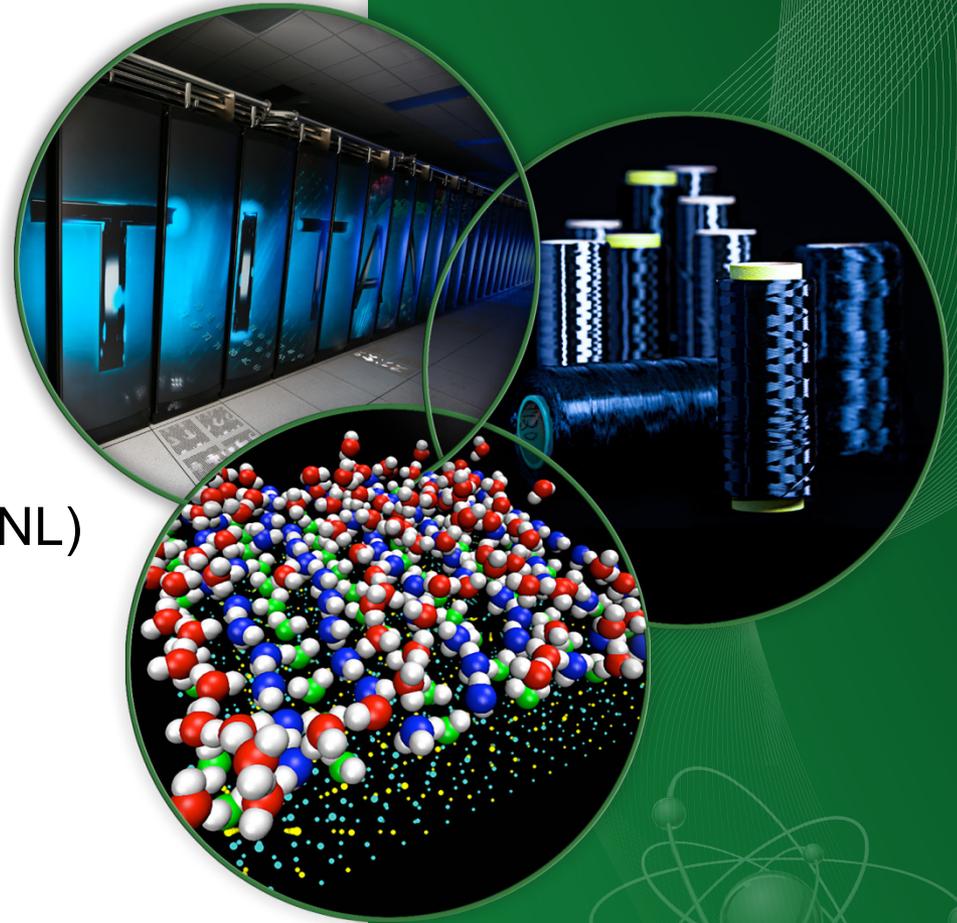


# Improvements for the $^{63}\text{Cu}$ and $^{65}\text{Cu}$ Resonance Evaluations for Criticality Safety Applications

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# Overview of Major Accomplishments in the Resolved Resonance Region Evaluation of $^{63}\text{Cu}$ and $^{65}\text{Cu}$

1. Experimental thermal cross section measurement
2. Resolved resonance region extended 3 x
3. Experimental capture data analyzed
4. High fidelity angular distribution generated



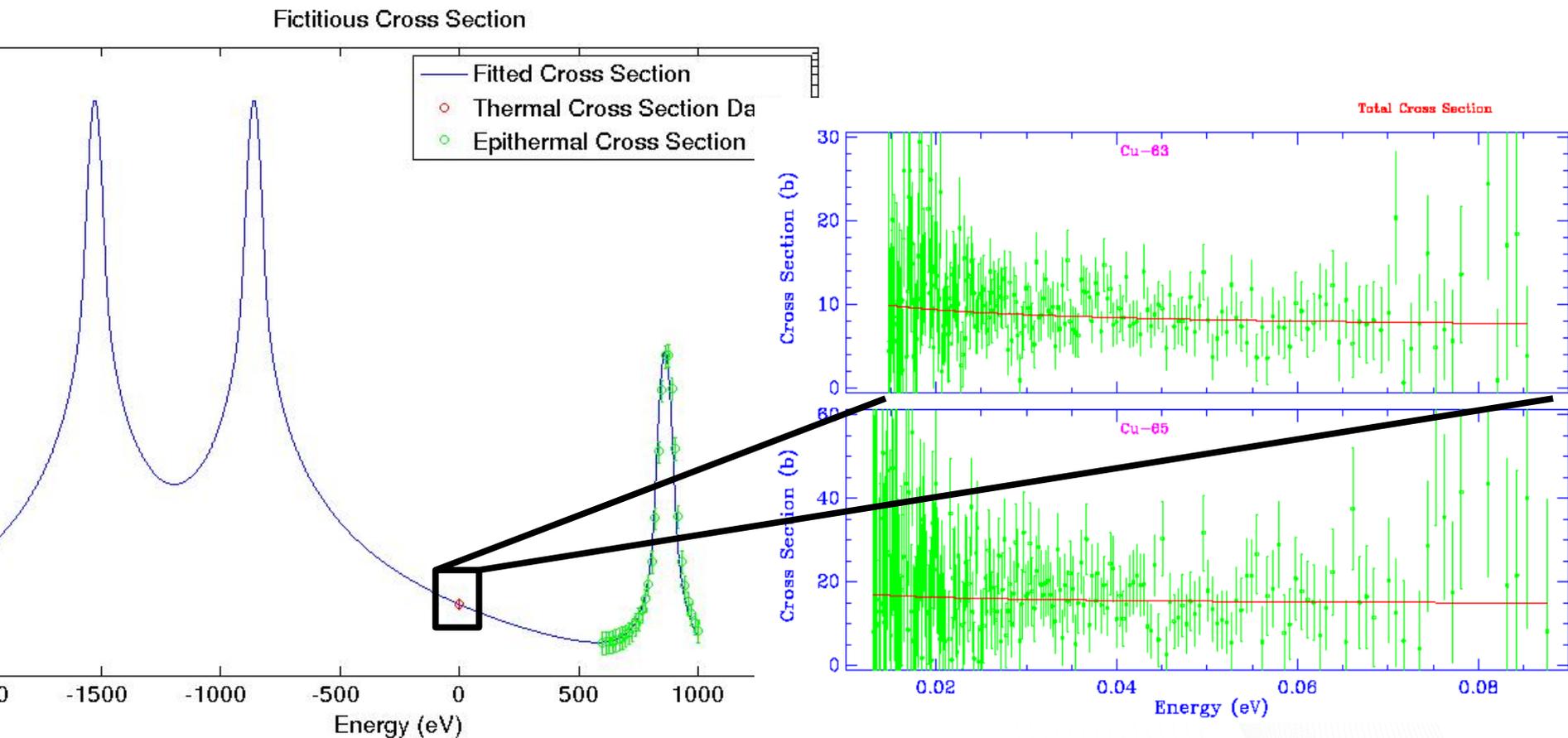
# SAMMY: Computer Code for R-Matrix Analysis

- Originally developed by ORNL to evaluate data from the ORELA experimental facility
- Currently used world wide for analysis of experimental cross section data
- Based on R-Matrix theory of nuclear reactions
- Uses Bayes's method (generalized least squares) to find optimal parameter values
- Generates uncertainty data for resonance region via Bayesian update method

## Experimental Data used in the New Evaluation

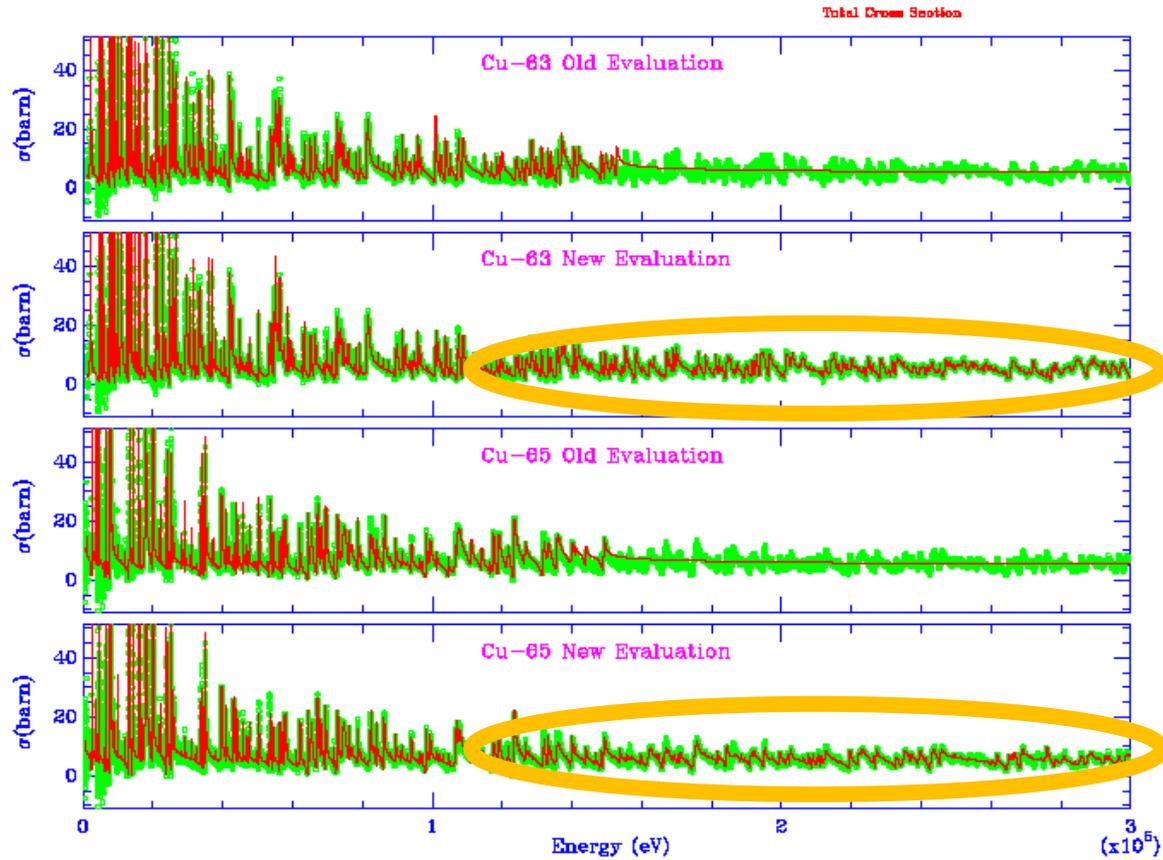
<b>Reference</b>	<b>Energy Range (eV)</b>	<b>Facility</b>	<b>Measurement</b>
Pandey et al.	32 – 185 000	ORELA	Trans. at 78 m
Pandey et al.	1 000 – 1 400 000	ORELA	Trans. at 78 m
Guber et al.	100 – 90 000	GELINA	Cap. at 58 m
Guber et al.	100 – 2 200 272	GELINA	Cap. at 58 m
Sobes et al.	0.01 – 0.1	MITR	Trans. at 1.2 m

# Thermal Cross Section Measurement to Define External Levels

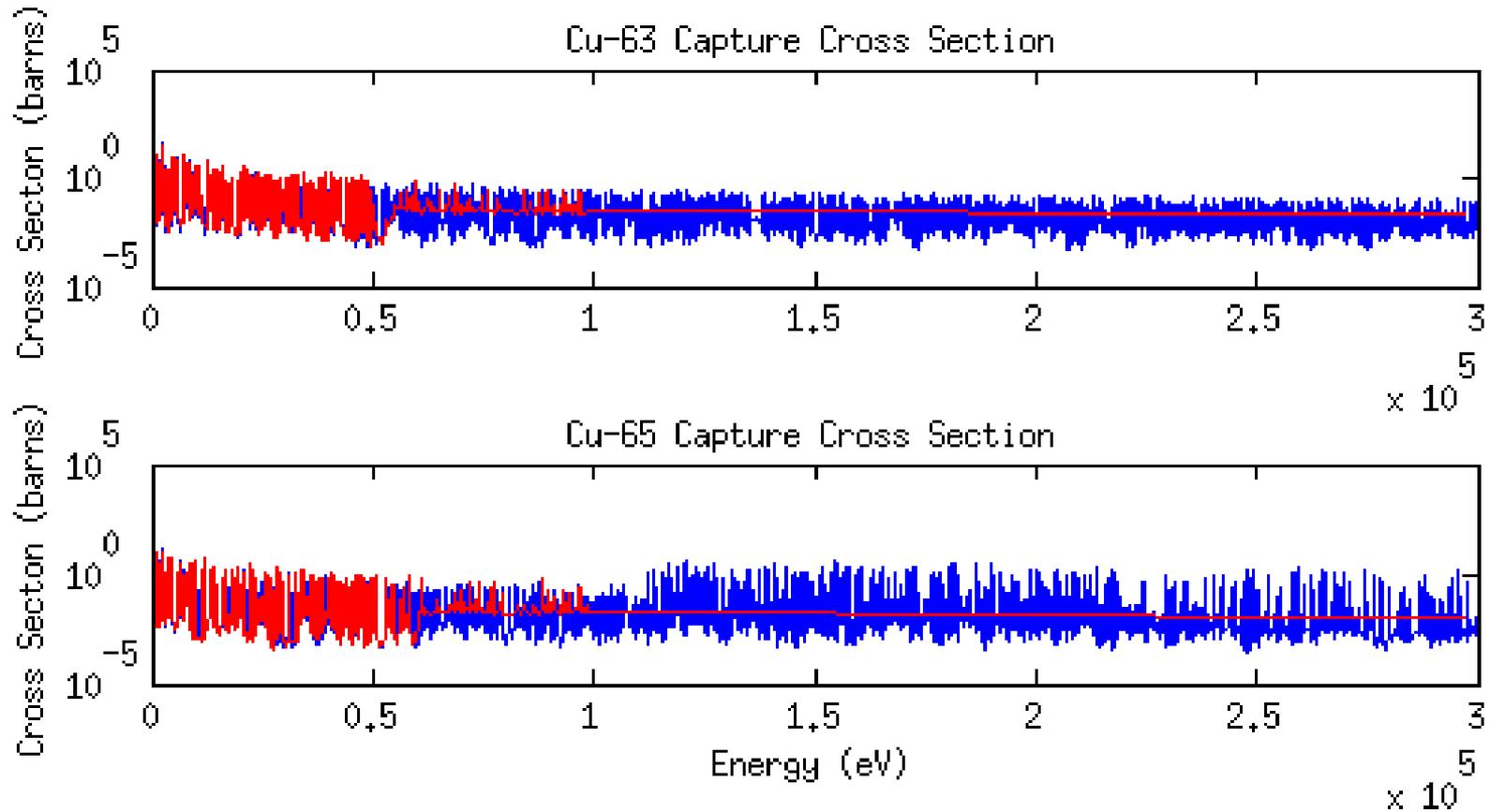


Much more definition of the negative external levels if we fit a differential cross section

# Extending the Resolved Resonance Region (Total Cross Section)

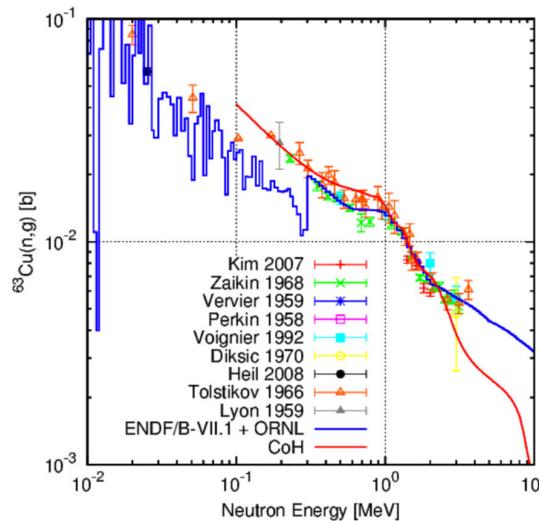


# Extending the Resolved Resonance Region (Capture Cross Section)

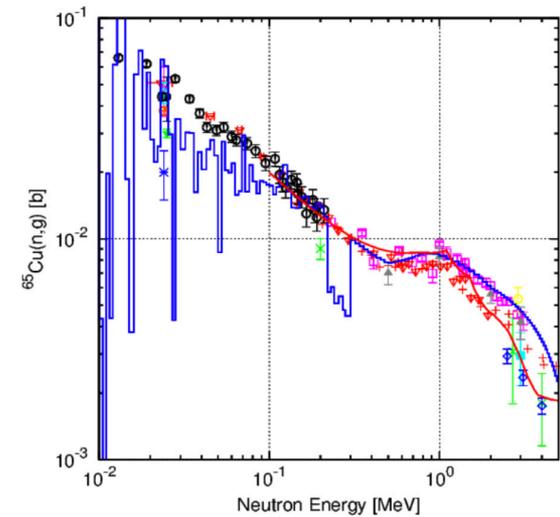


# Updated Resolved Resonance Region Evaluation: Updated Capture Cross Section $E > 220$ keV

- From Dr. Kawano,  
Mini CSEWG 2015

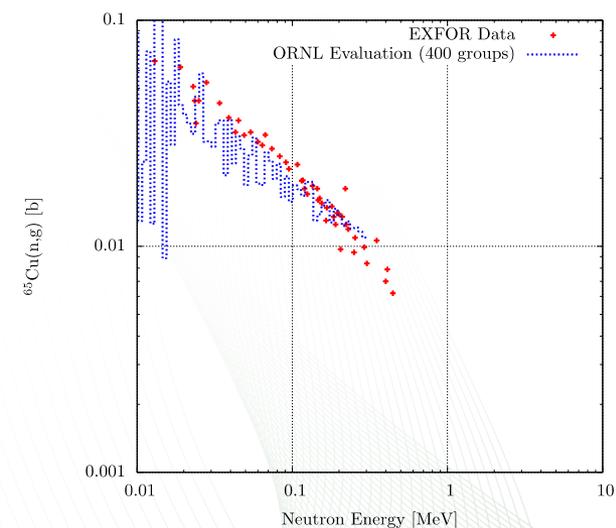
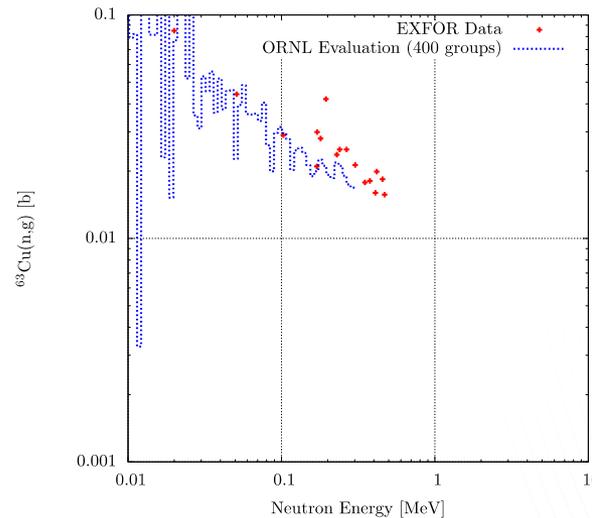


$^{63}\text{Cu}$  Capture Cross Section vs. Integral Measurements



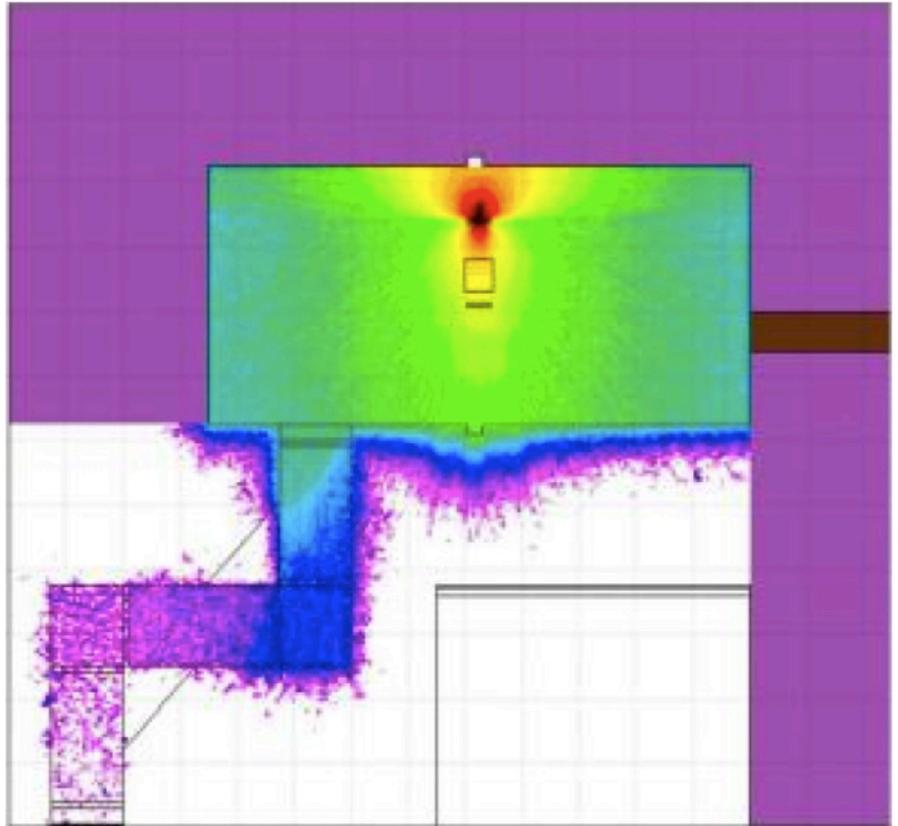
$^{65}\text{Cu}$  Capture Cross Section vs. Integral Measurements

- Corrected capture cross sections (in rev. 620 and 622 above 220 keV cross sections were underestimated)

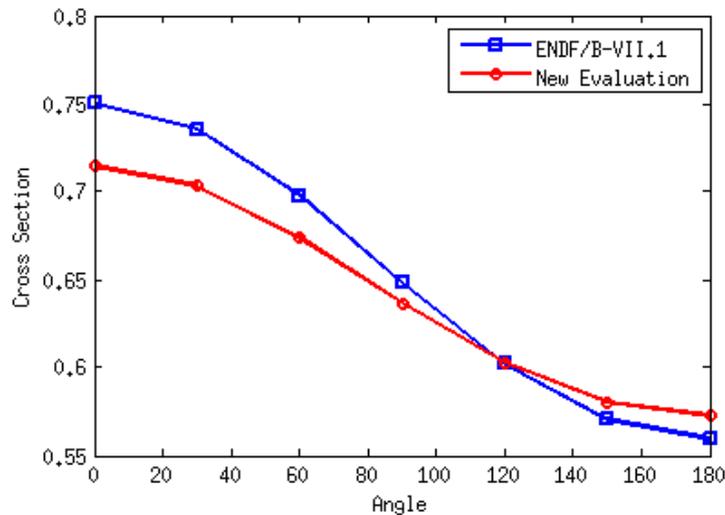
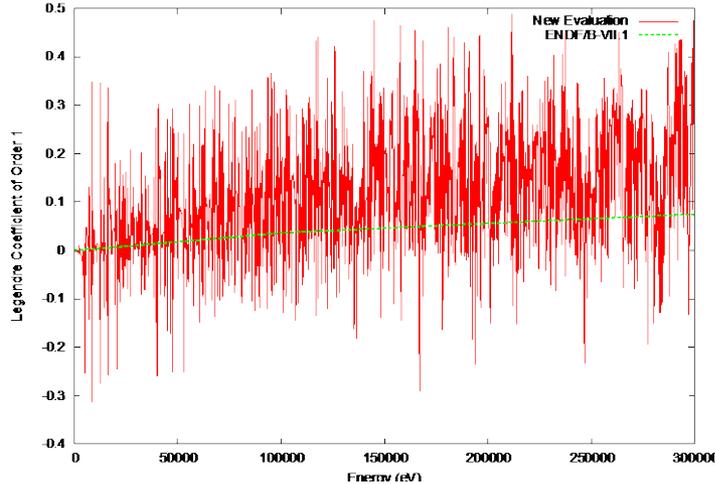


# Importance of Angular Distributions

- For radiation transport calculations, it can be crucially important to correctly understand which direction neutrons are more likely to travel after a scattering event
- NCS example:  
Analysis of criticality accident alarm system (CAAS) detector placement



# High Fidelity Model of Angular Distributions



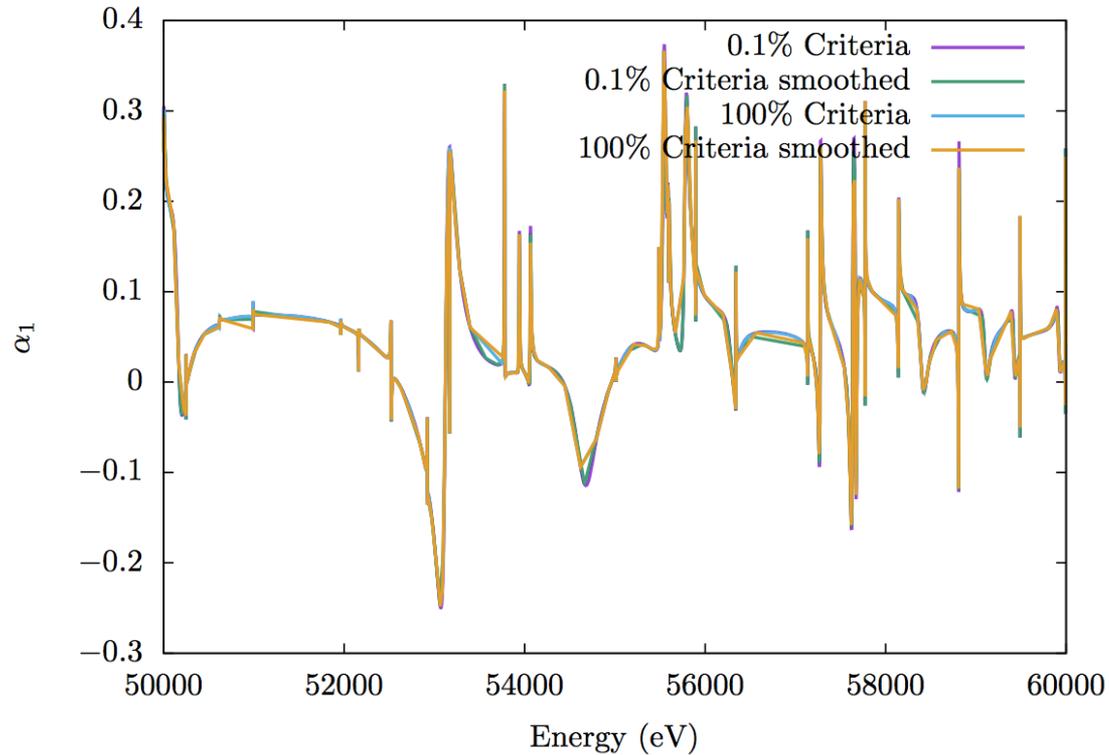
Differential cross section with respect to angle at E=60 keV for  $^{63}\text{Cu}(n,\text{els})$

- Angular distributions display physical resonances
- The average treatment leads to inconsistency between angle integrated cross sections and angular distributions

$$\alpha_l(E) = \frac{2\pi}{\sigma_s(E)} \int_{-1}^{+1} \sigma_s(E, \mu) P_l(\mu) d\mu$$

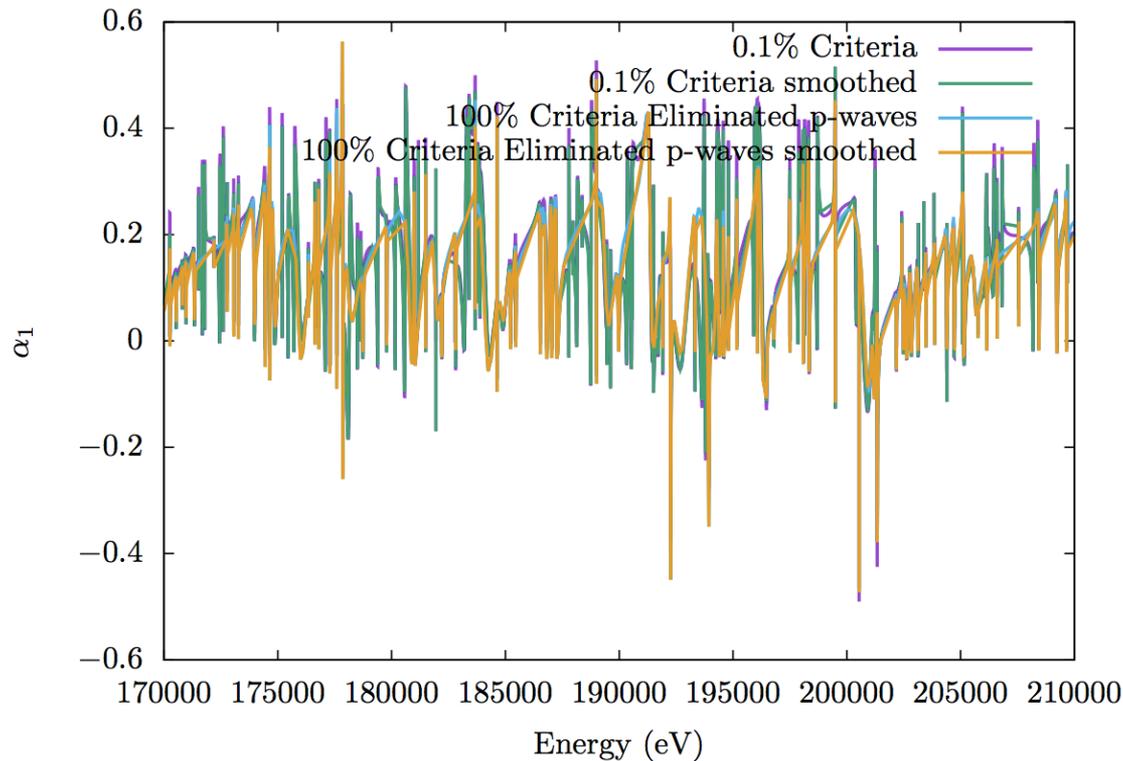
- $P_1(\mu) = \mu$
- $P_2(\mu) = 3/2\mu^2 - 1/2,$

# Smoothing of Angular Distributions: Joint effort with Luiz Leal (IRSN)



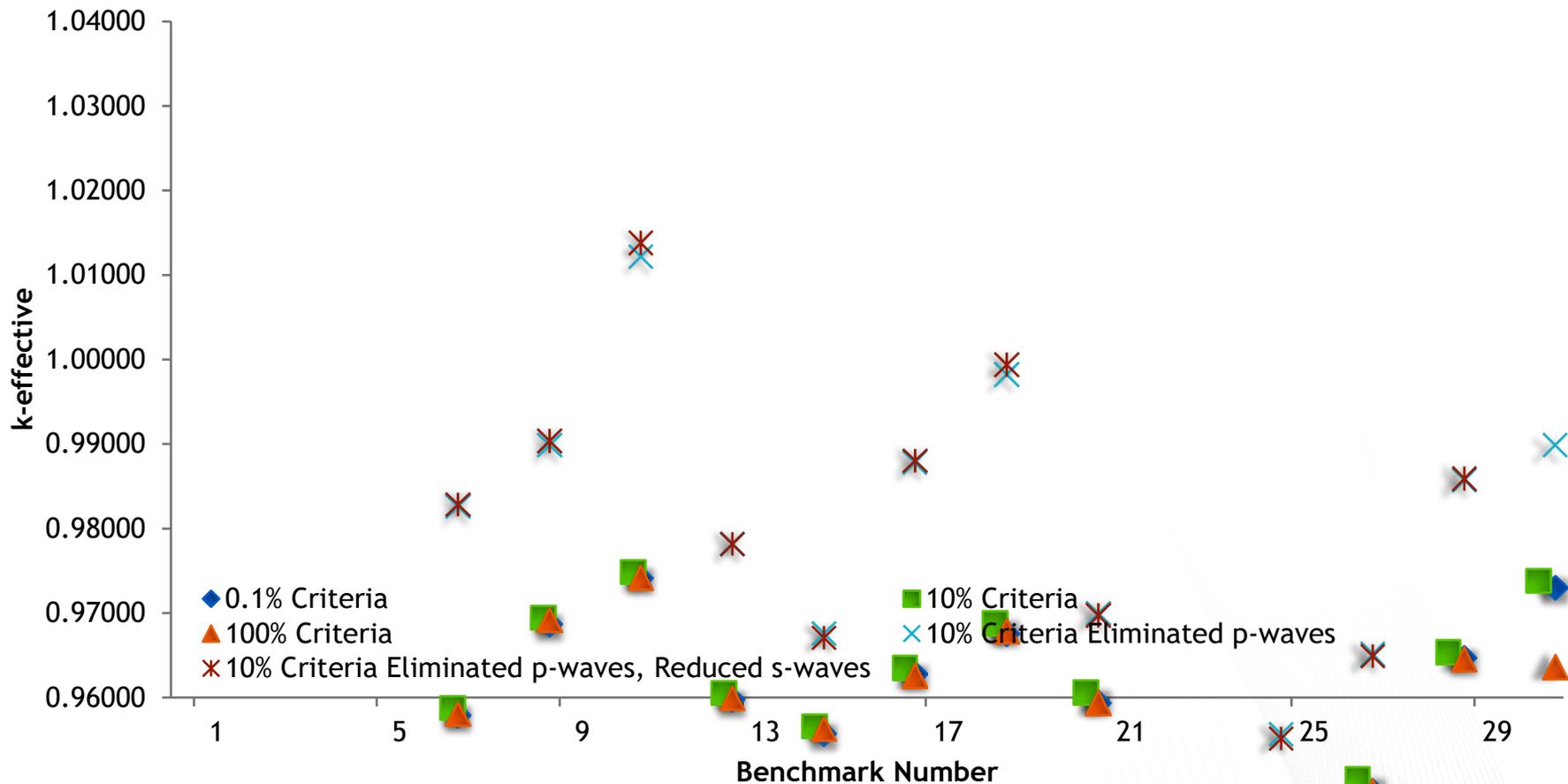
Interpolation Criteria	$^{63}\text{Cu}$		$^{65}\text{Cu}$	
		Smoothed		Smoothed
<b>0.1%</b>	83 467	10 373	65 922	7 943
<b>10%</b>	16 673	8 568	14 119	6 805
<b>100%</b>	11 440	7 078	10 341	5 758

## Smoothing of Angular Distributions: Joint effort with Luiz Leal (IRSN)



Interpolation Criteria	<sup>63</sup> Cu		<sup>65</sup> Cu	
	10%	100%	10%	100%
<b>Eliminated p-waves</b>	8 624	5 409	6 080	4 089
<b>Eliminated p-waves (smoothed)</b>	3 543	2 711	2 245	1 769
<b>Eliminated p-wave, Reduced s-waves</b>	5 366	2 756	3 417	1 850
<b>Eliminated p-wave, Reduced s-waves (smoothed)</b>	2 442	1 762	1 555	1 151

# Benchmark Results with Varying Fidelity of Angular Distributions

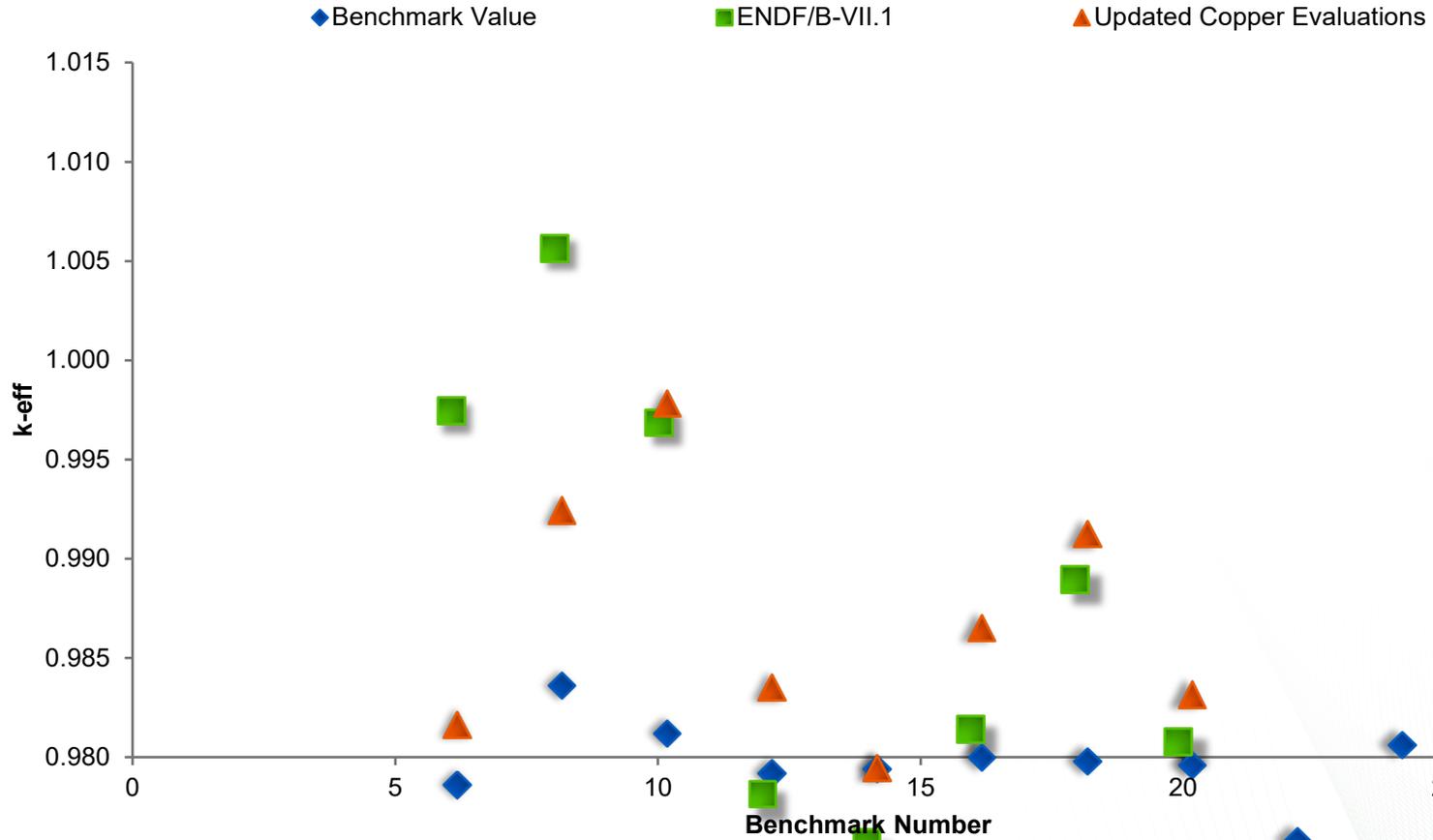


# Benchmark Table

Benchmark Number	ICSBEP Benchmark Name
1	HMF-72-01
2	HMF-72-03
3	HMF-73-01
4	HMF-84-06
5	HMF-84-18
6	HMF-85-01
7	HMF-85-02
8	HMF-85-04
9	HMI-06-01
10	HMI-06-02
11	HMI-06-03
12	HMI-06-04
13	IMF-20-01

Benchmark Number	ICSBEP Benchmark Name
14	IMF-20-02
15	IMF-20-03
16	IMF-20-04
17	IMF-20-05
18	IMF-20-06
19	IMF-20-07
20	IMF-22-01
21	IMF-22-05
22	IMF-22-06
23	IMF-22-07
24	IMI-01-02
25	IMI-01-03
26	IMI-01-04
27	PMF-40-01

# Overall Benchmark Results



# Conclusions

- Resolved Resonance Region Evaluations of  $^{63}\text{Cu}$  and  $^{65}\text{Cu}$ :
  1. Experimental thermal cross section measurement
  2. Resolved resonance region extended 3 x
  3. Experimental capture data analyzed
  4. High fidelity angular distribution generated
- Improvements for the  $^{63}\text{Cu}$  and  $^{65}\text{Cu}$  Resonance Evaluations
  1. Updated Capture Cross Section  $E > 220$  keV
  2. Reduced storage requirements for high fidelity angular distributions
  3. Benchmarked updated evaluations

# Improvements for the $^{63}\text{Cu}$ and $^{65}\text{Cu}$ Resonance Evaluations for Criticality Safety Applications

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