### **Resonance Region Quality Assurance**

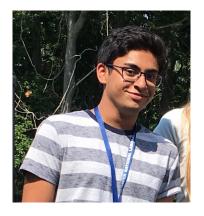
#### **David Brown**

NNDC, Brookhaven National Laboratory





#### My collaborators on this project





Rishi Wadgoankar (HSRP student)

Declan Mulhall (Univ. Scranton)





# ADVANCE continuous integration system key for ENDF QA

- Check new evaluations every commit
- Uses customer codes (NJOY, FUDGE, PREPRO)
- Automates ENDF Phase I testing
- Build reports for variety of needs



## In process of upgrading backend to Python3, BuildBot 2.10 on new server

• •		X Buildbot: builder build-alphas build 1 - Mozilla Firefox	
about:sessionrestore	×	S Buildbot: builder build-alp × +	
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Waterfall View		Build steps Build Properties Worker: workerCP Responsible Users Change	s Debug
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Build Masters		41 PWD=/home/dbrown/advance.trunk/work/endf/workerCP/build-alphas/buil 42 PYTHONPATH=/home/dbrown/fudge.trunk:/home/dbrown/advance.trunk:/home/dbrown/adv	
Schedulers		<pre>43 QTDIR=/usr/lib64/qt-3.3 44 QTINC=/usr/lib64/qt-3.3/include</pre>	
Workers		45 QTLIB=/usr/lib64/qt-3.3/lib 46 QT_GRAPHICSSYSTEM_CHECKED=1	
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## In process of upgrading backend to Python3, BuildBot 2.10 on new server

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Build Masters		<pre>41 PWD=/home/dbrown/advance.trunk/work/endf/workerCP/build-alphas/build 42 PYTHONPATH=/home/dbrown/fudge.trunk:/home/dbrown/advance.trunk:/home/dbrown/</pre>	own/x4i.trunk:		
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Workers		45 QTLIB=/usr/lib64/qt-3.3/lib 46 QT_GRAPHICSSYSTEM_CHECKED=1			
About	0	<ul> <li>47 QT_PLUGIN_PATH=/usr/lib64/kde4/plugins:/usr/lib/kde4/plugins</li> <li>48 SELINUX_LEVEL_REQUESTED=</li> <li>49 SELINUX_ROLE_REQUESTED=</li> </ul>			
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		55 SSH TTY=/dev/nts/0			4

TOR







- Missing resonances
- Miss-assigned resonances

Focus of this work





- Missing resonances
- Miss-assigned resonances
- Missing or incorrect backgrounds
- Bad fits to experiment

#### Focus of this work

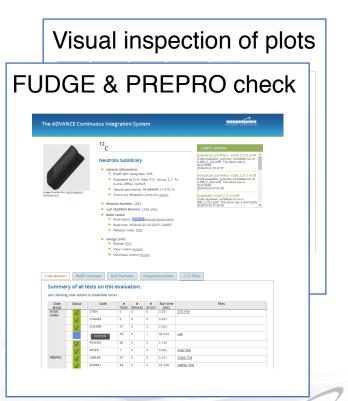
Code Results	ENDF Overview	ACE Overview	Integral Quantit		
1 - C - C - C - C - C - C - C - C - C -	taken from the EXFOR IB				in a plot legend
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- Missing resonances
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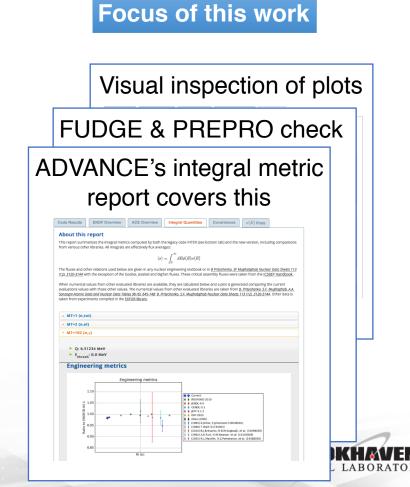




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- Missing resonances
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- Bad match to integral quantities (RI, thermal cross section, MACS, Westcott factor, ...)



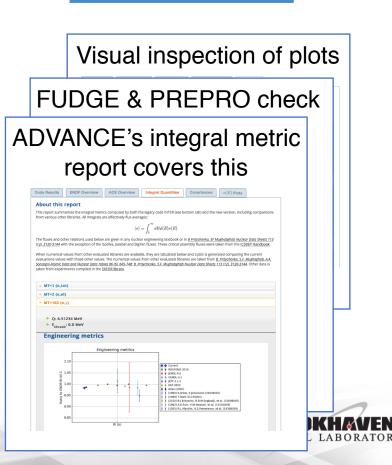


- Missing resonances
- Miss-assigned resonances
- Missing or incorrect backgrounds
- Bad fits to experiment
- Missing channels
- Bad match to integral quantities (RI, thermal cross section, MACS, Westcott factor, ...)
- Inconsistent with the Atlas
- RRR-URR inconsistency

#### Working on it!



#### Focus of this work



### **Resonance metrics to consider**

#### **Measures of energies**

- Long range behavior
  - Average spacing vs. E
  - Cumulative level distribution

#### Short range behavior

- Nearest neighbor spacing distribution
- Spacing-spacing correlation
- Dyson-Mehta ∆<sub>3</sub> statistic
- Other statistics

#### Measures of widths

- Long range behavior
  - Average width vs. E
  - Width distribution

#### Short range behavior

• Are there short range correlations in the widths?



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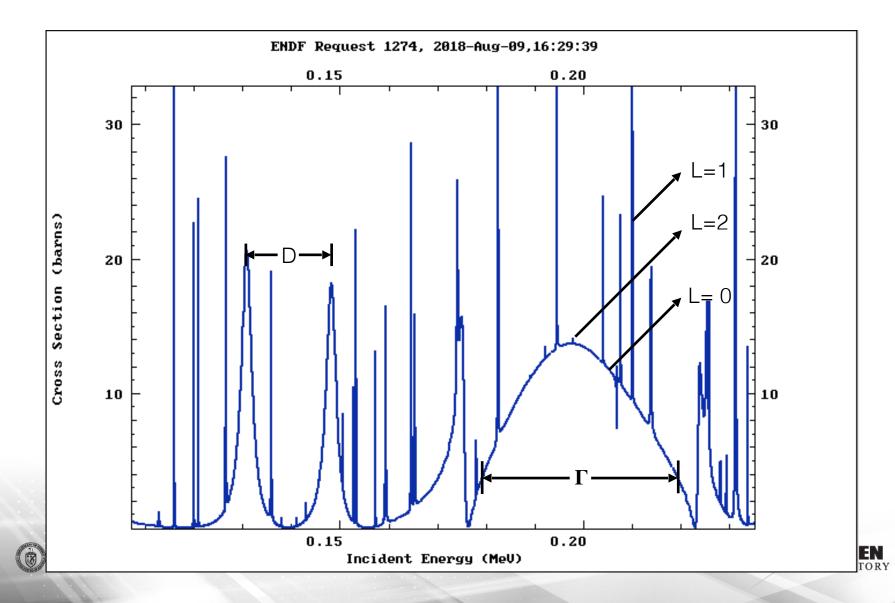
• Are there short range correlations in the widths?

In most cases, have analytic results from random matrix theory as guide





### **Typical resonance region**



### **Resonance metrics to consider**

#### **Measures of energies**

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- Cumulative level distribution

#### Short range behavior

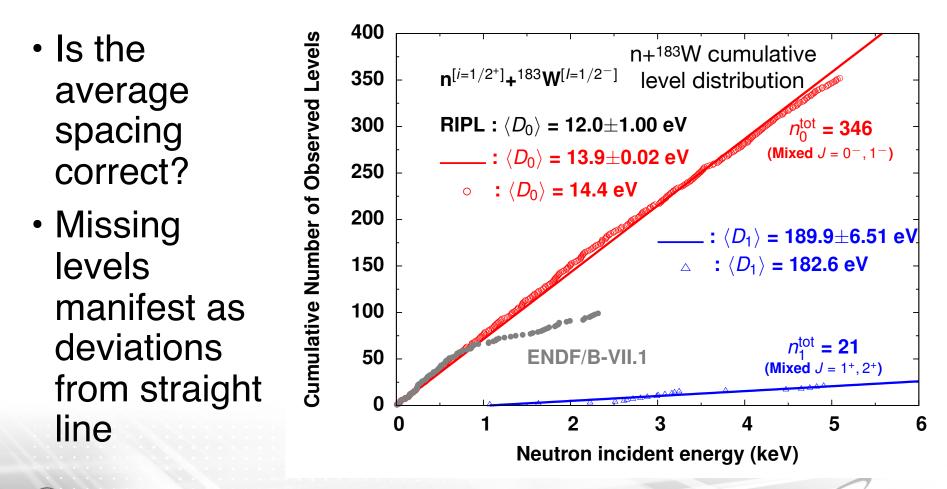
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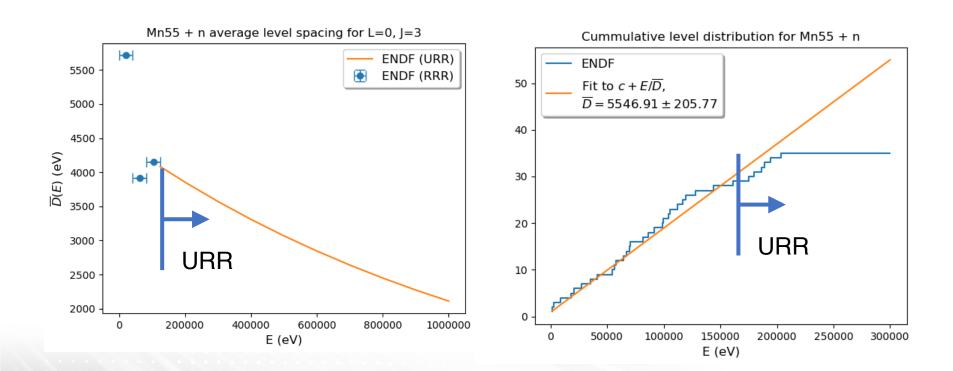


# Cumulative level distribution already tells us a lot



D. Brown, et al. Nucl. Data Sheets 148, 1 (2018)

### Application to <sup>55</sup>Mn shows good RRR-URR transition; before missing lots of levels







### Look at resonance spacings

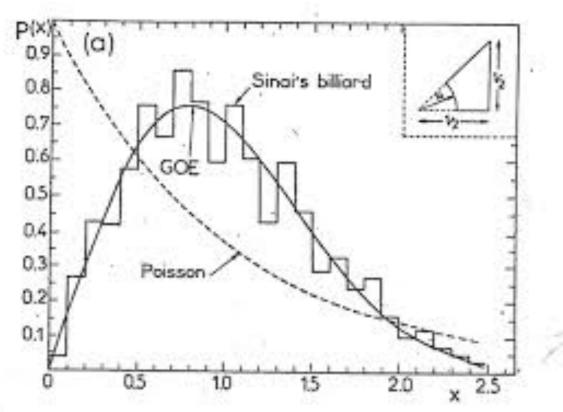
a	Ъ	с	d	e	f
Poisson	Primes	n+"Er	Sinai	 Zeros ζ(s)	Uniform

O. Bohigas and M. J. Giannoni, Lecture Notes in Physics 209 (1984), Springer-Verlag, Heidelberg





## Nearest neighbor spacing distribution



Nearest neighbor spacing is simply

$$D_i = E_{i+1} - E_i$$

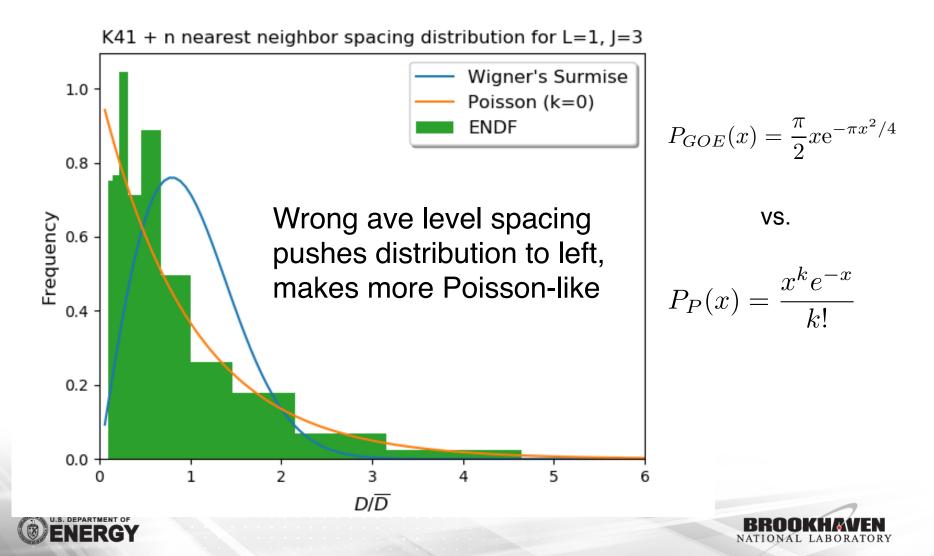
So, make a histogram with

 $x=D_i/D$ 

Bohigas, Giannoni, Schmitt, Phys. Rev. Lett. 52, p. 1 (1984)

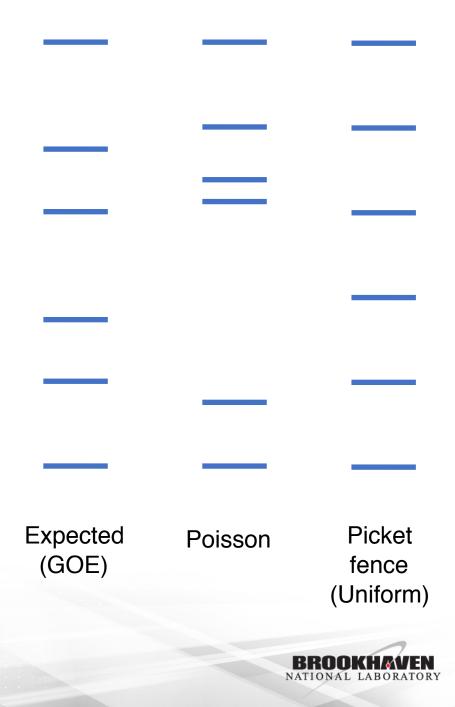


### Can immediately tell that levels are missing based on shape or shift in x-axis scaling



# Spacings tell us a lot more

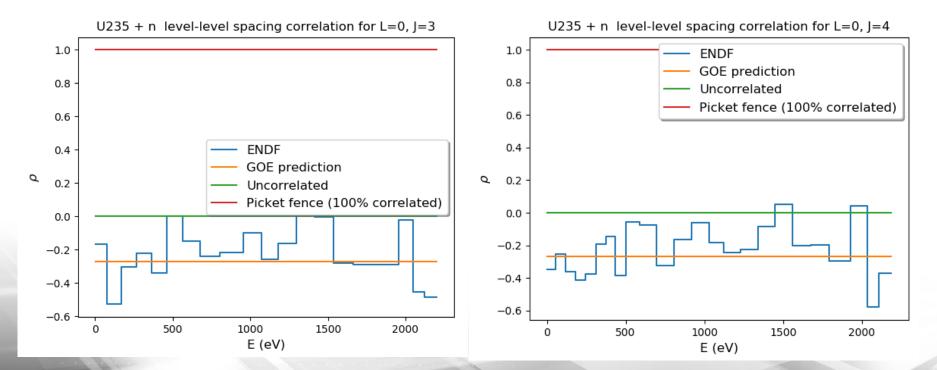
- Poisson too random: has big gaps and big clusters
- Picket fence too regular
- GOE just right
  - S-L-S-L spacing correlation
  - Almost as regular as picket fence





### $\rho$ , the spacing-spacing correlation $\rho(D_i, D_{i+1}) = \operatorname{corr}(D_i, D_{i+1})$ $= \frac{\sum_i (D_i - \overline{D})(D_{i+1} - \overline{D})}{\sum_i (D_i - \overline{D})^2}$

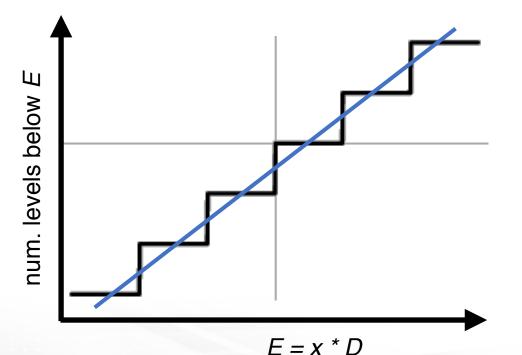
S-L-S-L pattern gives correlation coefficient of -0.27 for GOE



### **Dyson-Mehta** $\Delta_3$ statistic

- A fancy sounding name
- Measures "spectral stiffness"
- Really just based on straight line fit to cumulative level distribution
- Vary number of steps
   (L) used in fit
- Know expected slope as function of L

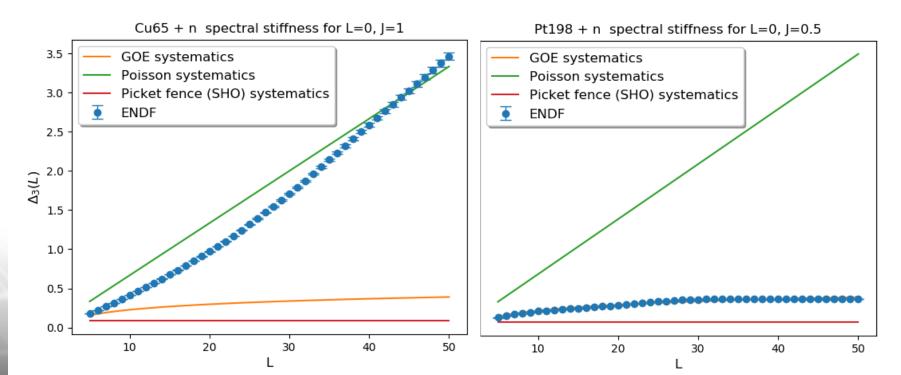
$$\Delta_{3}(r) = \frac{d}{2L} \min_{A,B} \int_{x-L}^{x+L} [F(x') - Ax' - B]^{2} dx'$$





### **Dyson-Mehta** $\Delta_3$ statistic

- Know expected values of  $\Delta_3$  for picket fence (regular), GOE (realistic) and Poisson (random)
- 65Cu indicates significant admixture of resonances from other channel
- <sup>198</sup>Pt does NOT indicate complete set of resonances, rather indicates quality of fake resonances generated by TARES



### **Other metrics**

- U statistic "thermodynamic energy"
- Q statistic
- F statistic

• All give essentially same information as  $\Delta_3$ 





### **Resonance metrics to consider**

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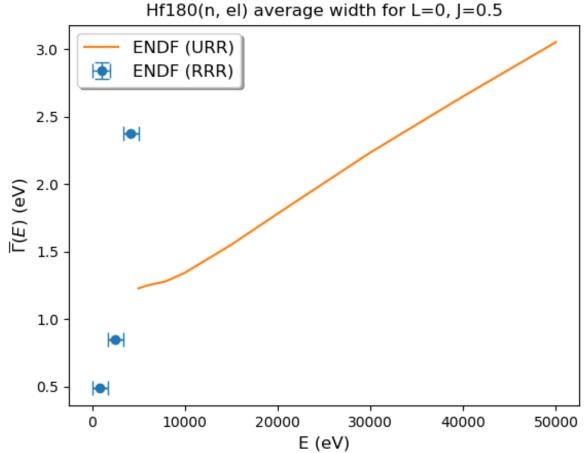
• Are there short range correlations in the widths?





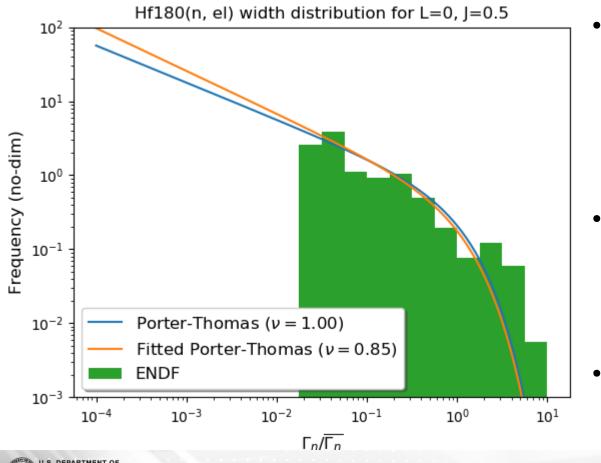
# Plot average with to show consistency between RRR & URR

- Gamma widths usually small, not vary much
- Neutron widths, must be careful about "reduced width" in URR



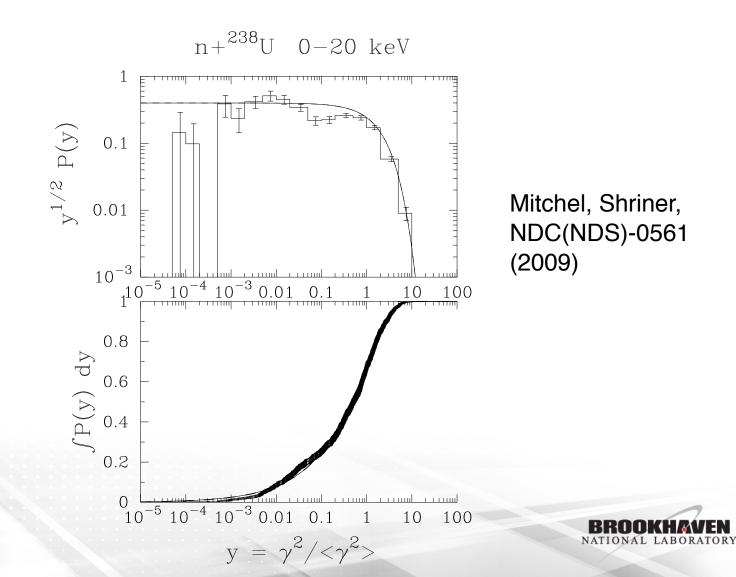


# Width distribution commonly used to assess for missing levels



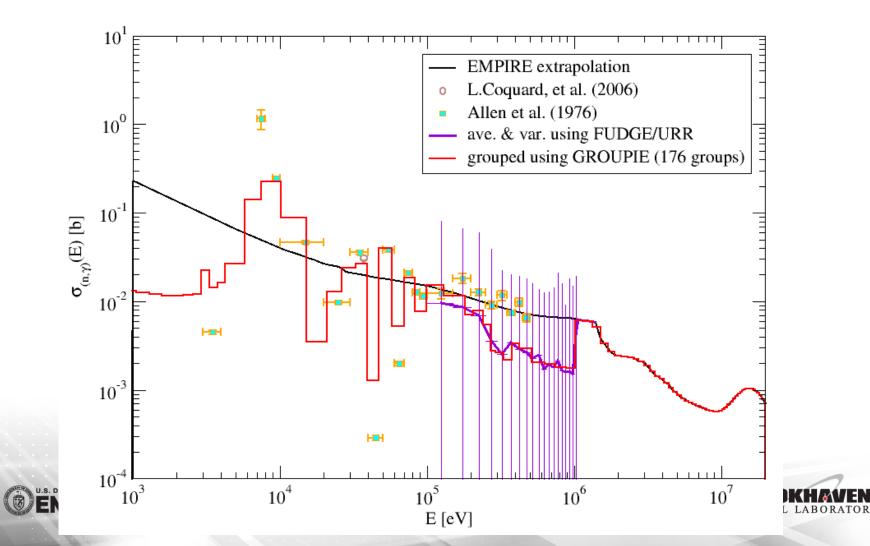
- A lot of literature using this to assess missing levels
- Wrong ave width pushes distribution to left
- Missing levels have small width

### Other ways of displaying width distribution are more informative, must investigate

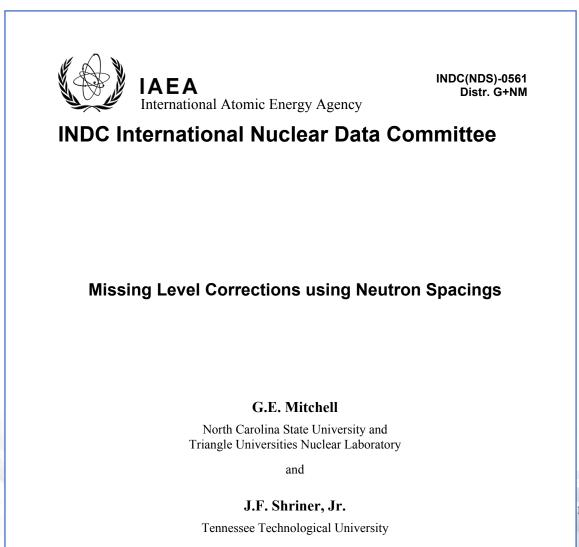




#### <sup>54</sup>Fe capture: group averaged capture resonances reveals missing strength from 200 keV - 1 MeV, likely from missing p-, d- wave resonances



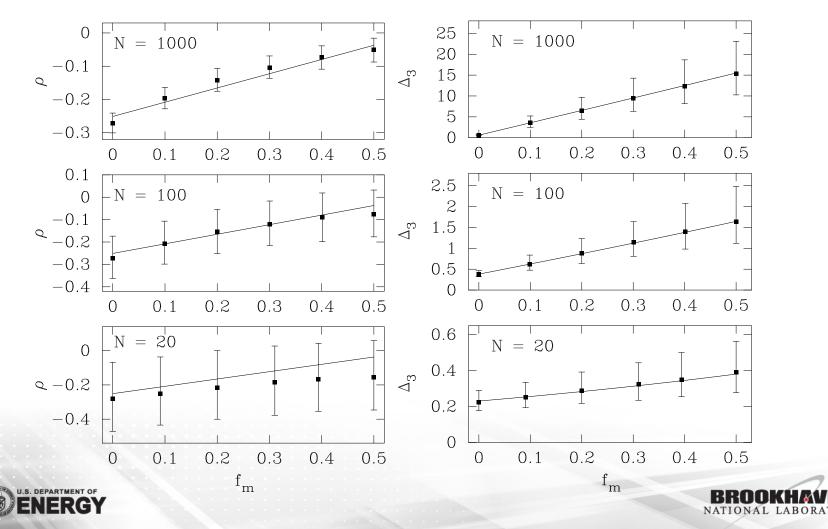
# Mitchell and Shriner missing level study INDC(NDS)-0561





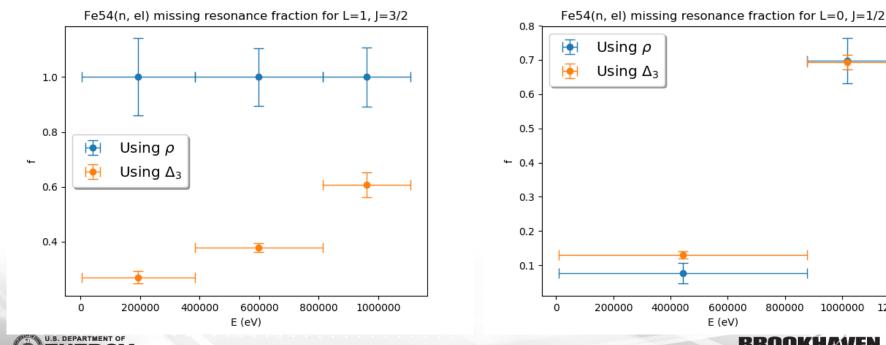


# Systematics of $\rho$ & $\Delta_3$ as function of # levels & fraction missing

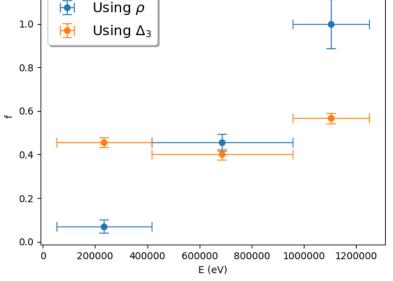


Fe54(n, el) missing resonance fraction for L=1, J=1/2

### Can we use these to assess the fraction of missing resonances?







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1000000

1200000

800000

600000

E (eV)

### Status

- Lab report detailing system available (BNL-209313-2018-INRE)
- Aiming for rollout of report before next CSEWG
- Investigating combining width & Dyson-Mehta metrics for more holistic estimate of missing/miss assigned levels
- Investigating RRR-URR constancy approaches

