## Angular distributions in ENDF/B-VIII. 0

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Office of Science

## The scattering angular distribution can have dramatic impact on small systems

## ${ }^{23} \mathrm{Na}$ elastic SAD

Figures from
G. Noguerre, C. Jouanne, O. Leray, P. Archier, and C. Vaglio-Gaudard. "Elastic
Scattering
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The Fast
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Moulineaux. 22
May 2013.
OECD-NEA.
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SAD with a smooth fit of the $a_{1}$ coefficient

## Two-body angular distributions are calculable, analytically, using BlattBeidenharn formalism

$$
\begin{equation*}
\frac{d \bar{\sigma}_{a \rightarrow b}}{d \Omega_{b}}=\left(\frac{2 \pi}{\hbar}\right)^{4} \mu_{a} \mu_{b} \frac{k_{b}}{k_{a}} \frac{1}{2 I_{x}+1} \frac{1}{2 I_{A}+1} \sum_{L=0}^{\infty} B_{L}\left(\underline{b}, \underline{a} ; E_{a}\right) P_{L}(\mu) \tag{15}
\end{equation*}
$$

$B_{L}\left(\underline{b}, \underline{a} ; E_{a}\right)=\sum_{S_{a}, S_{b}} \frac{(-)^{S_{b}-S_{a}}}{4} \sum_{J \ell_{a} \ell_{b}} \sum_{J^{\prime} \ell_{a}^{\prime} \ell_{b}^{\prime}} \bar{Z}\left(\ell_{a} J \ell_{a}^{\prime} J^{\prime} ; S_{a} L\right) \bar{Z}\left(\ell_{b} J \ell_{b}^{\prime} J^{\prime} ; S_{b} L\right) \Re\left[T_{\left\{a ; ;_{a}, S_{a}\right\} \rightarrow\left\{b ; \ell_{b} S_{b}\right\}}^{J} T_{\left\{a ; \ell_{a}^{\prime} S_{a}\right\} \rightarrow\left\{b ; b_{b}^{\prime} S_{b}\right\}}^{J^{\prime}}\right]$.
$\bar{Z}\left(\ell_{a} J \ell_{a}^{\prime} J^{\prime} ; S_{a} L\right)=\sqrt{\left(2 \ell_{a}+1\right)\left(2 \ell_{a}^{\prime}+1\right)(2 J+1)\left(2 J^{\prime}+1\right)}\left(\ell_{a} 0 \ell_{a}^{\prime} 0 \mid L 0\right) \mathcal{W}\left(\ell_{a} J \ell_{a}^{\prime} J^{\prime} ; S_{a} L\right)$
$\mathcal{W}\left(\ell_{a} J \ell_{a}^{\prime} J^{\prime} ; S_{a} L\right)=(-1)^{-\left(\ell_{a}+\ell_{a}^{\prime}+J+J^{\prime}\right)}\left\{\begin{array}{ccc}\ell_{a} & J & S_{a} \\ J^{\prime} & \ell_{a}^{\prime} & L\end{array}\right\}$

- It's ugly, but well understood.
- Implemented in FUDGE, EMPIRE, CoH, SAMMY, AMPX, NJOY, ....


## ${ }^{63} \mathrm{Cu}\left({ }^{65} \mathrm{Cu}\right.$ is similar)

Legendre Moment for Cu63(n,el)


- Smoothed distribution in excellent agreement with reconstructed distribution. - is actually no surprise: FUDGE \& SAMMY used these data to validate against each other


## Justin Vega's project

- BNL's High School Research Program
- Final report is huge, available upon request. Report number BNL-114446-2017-IR
- The project:
- Test that energy average SAD approaches HF SAD
- Check all SAD in ENDF/B-VIII. 0 beta3



# Issues encountered in full library scan (ENDF trackers have been added for each of these) 

## Anomaly in Si isotopes



- All isotopes have same distribution, taken from ENDF/B-V natSi
- Natural SAD built from isotopic SADs
- If SAD is smooth, is OK to replace isotopic with natural SADs
- THIS IS NOT THE CASE


## Anomaly in Cr isotopes

Legendre Moment for Cr50(n,el)


Legendre Moment for Cr53(n,el)


Legendre Moment for Cr52(n,el)



- Same issue as Si
- May be part of problem with steel assemblies


## ${ }^{101} R \mathrm{u},{ }^{105} \mathrm{Pd}$, ${ }^{109} \mathrm{Ag},{ }^{108,110,116} \mathrm{Cd}, 131 \mathrm{Xe}$, ${ }^{133} \mathrm{Cs}$, ${ }^{141} \mathrm{Pr}$ <br> Legendre Moment for Ru101(n,el)



- Symmetry requires that, as $\mathrm{E} \rightarrow 0, \mathrm{P}_{\mathrm{L}=0}(\mu) \rightarrow 0$
- Several isotopes violate this requirement


## xTI, xPb, ${ }^{209} \mathrm{Bi}$

Legendre Moment for Pb208(n,el)



- Here agreement is poor
- Near closed shell, fluctuations large, extend to high energy
- May indicate problem with OMP's involved
- Requires further investigation


## BNL Report BNL-114446-2017-IR

Scattering Angular Distributions in the ENDF/B Nuclear Data Library

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Nuclear reactors function by controlling the chain reaction of fission events in a fissile material. Understanding the gain and loss of neutrons is crucial for controlling this chain reaction. The role of fission in liberating neutrons from nuclei is well known. The fact that neutrons can scatter out of a reactor and therefore be lost is less well appreciated. Scattering can happen within fissile fuel or off of any number of the non-fissile structural components holding a reactor together. The scattering angular distributions for reactor material are the quantity that give the probability for a particle (usually a neutron) to scatter off a nucleus into a given angle. The Evaluated Nuclear Data File/B (ENDF/B) nuclear data library is the most complete and authoritative reference for neutron scattering data, containing reaction cross sections and outgoing particle distributions (including scattering angular distributions). In this project, we will compare the scattering angular distributions given in these ENDF/B data sets with those that can be derived using the Blatt-Biedenharn formalism and the resolved resonance data also in the ENDF/B files. More comparisons between the scattering angular distributions of relevant isotopes will help identify and correct any errors in the ENDF/B files. The results of this study will be an important component of the next major release of the ENDF/B library.

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